

Name _____

College Pre-Calc

Final Exam Review #2

1. Find the inverse of the function $f(x) = \sqrt{2x-3}$ in the form $f^{-1}(x) =$
2. Determine the intervals on which the function $y = -x^2 + 6x - 8$ is increasing, decreasing or constant.
3. If $f(x) = 2x - 3$ and $g(x) = 8x^2$, find $(g \circ f)(x)$.
4. Find all asymptotes of the function $f(x) = \frac{x^3 - 3x - 14}{x^2 - 4x - 5}$.
5. Given the equation $729 = 8^{-2-x}$, solve for x.
6. Expand $\log_2 \frac{x^2 \sqrt{y}}{w^3}$
7. Find the derivative of $f(x) = x^4 - x^2 + 1$ at $(2, 13)$.
8. Find the limit of $\lim_{x \rightarrow 2} \frac{4 - \sqrt{18-x}}{x-2}$, if it exists.
9. Find $f'(x)$ and write the equation of the tangent line at $(2, 5)$ in point-slope form:
$$f(x) = 2x^2 - x - 1$$
10. Find the difference quotient and simplify:
$$f(x) = 2x^3 - x + 2, \quad \frac{f(x+h) - f(x)}{h}, h \neq 0$$

11. Find the equation for the hyperbola given the information below:

$$\text{center: } (4, 5)$$

$$\text{foci: } (4, 10)$$

$$\text{vertex: } (4, 9)$$

Factor:

$$12. \quad a^3 + 27$$

$$13. \quad x^6 - 2x^4 + 3x^2 - 6$$

$$14. \quad m^6 - 25n^8$$

$$15. \quad \text{Expand } (3x+2)^4$$

16. Determine if $3x+1$ is a factor of $6x^2 - 13x + 5$, by using long division. Explain your answer.

Simplify each expression using positive exponents only.

$$17. \quad \frac{4x^8 \bullet -x^2}{32x^7}$$

$$18. \quad \left(\frac{3x^{-2}y^9}{z} \right)^{-3}$$

$$19. \quad \text{Simplify: } \frac{\frac{3}{x^2} + \frac{1}{x}}{1 - \frac{9}{x^2}}$$