

Final Exam Review #5

1. Determine if $g(x) = \begin{cases} -x^2 + 4 & x \leq 1 \\ 6x - 1 & x > 1 \end{cases}$ is continuous at $x = 1$

2. Find the value of b for which $h(x) = \begin{cases} 5x - 7 & x \leq -1 \\ b + 4x & x > -1 \end{cases}$ is continuous at $x = -1$

3. Using $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$
 - a) Find the derivative of $f(x) = 2x^2 - 3x$
 - b) Find the equations of the tangent & normal lines at $x = -3$

4. Complete the square to find the standard form of the ellipse. Find the center, foci and vertices.
$$x^2 + 9y^2 + 8x - 18y + 16 = 0$$

5. Verify the identity: $\frac{\csc x}{\sin x} - \frac{\cot x}{\tan x} = 1$

6. In $\triangle ABC$, $a = 24$, $b = 36$ and $c = 30$. Find $m\angle A$ to the nearest tenth of a degree.

7. In $\triangle ABC$, $m\angle A = 40$, $m\angle C = 65$ and $c = 12$. Find the length of a to the nearest integer.

8. Two forces act on a body at an angle of 100° . The forces are 30 pounds and 40 pounds.
 - a) Find the magnitude of the resultant force to the nearest tenth of a pound.
 - b) Find the angle formed by the greater of the two forces and the resultant force to the nearest degree.

9. Solve the system of equations:
$$\begin{aligned} 4x - 3y + z &= -10 \\ 2x + y + 3z &= 0 \\ -x + 2y - 5z &= 17 \end{aligned}$$