

Name: Answer Key  
Ms. Schmidt

Pd \_\_\_\_\_

Date \_\_\_\_\_  
Intermediate Algebra

Review for Exam #1

Notes	Examples									
<p><b>Combining Like Terms</b> -Match the variables and exponents -Add and subtract the coefficients **Exponents STAY the same!</p>	<p>1) <math>\frac{5}{2}x^2 + \frac{1}{4}x - \frac{1}{5}x^2 + \frac{3}{8}x - \frac{5}{2}</math> <math>\frac{23}{10}x^2 + \frac{5}{8}x - \frac{5}{2}</math></p>									
<p><b>Distributing</b> -Multiply the number outside of the ( ) or     inside -Combine like terms AFTER distributing</p>	<p>2) <math>5[x - 3(2x - 4)]</math> <math>5[x - 6x + 12]</math> <math>5x - 30x + 60 \rightarrow -25x + 60</math></p>									
<p><b>Evaluating Expressions/Functions</b> -Replace the variables with the numbers using ( ) -Type into calculator using ( )!!!</p>	<p>3) Evaluate <math>a^2 - abc + b</math> when <math>a = -1, b = 2, c = -3</math> <math>(-1)^2 - (-1)(2)(-3) + 2 = -3</math> 4) If <math>f(x) = x^3 - 4x^2 + 1</math> find <math>f(-2)</math> <math>(-2)^3 - 4(-2)^2 + 1 = -23</math></p>									
<p><b>Adding Polynomials</b> -Combing like terms!!! <i>*descending order*</i></p>	<p>4) Find the sum of <math>(3x^3 + 4x^2 - 5x)</math> and <math>(5x^2 - 6x^3 + 8x)</math> <math>-9x^3 + 9x^2 + 3x</math></p>									
<p><b>Subtracting Polynomials</b> -Keep the first polynomial the same -Change to addition -Change ALL signs in the second polynomial **FROM means FIRST! <i>*descending order*</i></p>	<p>5) Subtract <math>-3x^3 + 4x^2 - 5x</math> from <math>5x^2 - 6x^3 + 8x</math> An <math>(5x^2 - 6x^3 + 8x) + (3x^3 - 4x^2 + 5x)</math> <math>-3x^3 + x^2 + 13x</math> 6) Subtract: <math>(6x^2 - 5x + 2) - (5x^2 - 4x - 6)</math> <math>(6x^2 - 5x + 2) + (-5x^2 + 4x + 6)</math> <math>x^2 - 9x + 8</math></p>									
<p><b>Multiplying Polynomials</b> -Multiply the coefficients -Add the exponents *Double distribute or Box Method!!</p>	<p>7) <math>(2x - 5)(x + 5)</math> <math>2x^2 + 10x - 5x - 25</math> <math>2x^2 + 5x - 25</math> 8) <math>(x^2 - 4)(x^3 - 5x + 12)</math> <table border="1" style="display: inline-table; vertical-align: middle;"> <tr><td><math>x^3</math></td><td><math>x^5</math></td><td><math>-4x^3</math></td></tr> <tr><td><math>-5x</math></td><td><math>-5x^3</math></td><td><math>+20x</math></td></tr> <tr><td><math>+12</math></td><td><math>12x^2</math></td><td><math>-48</math></td></tr> </table> <math>x^5 - 9x^3 + 12x^2 + 20x - 48</math></p>	$x^3$	$x^5$	$-4x^3$	$-5x$	$-5x^3$	$+20x$	$+12$	$12x^2$	$-48$
$x^3$	$x^5$	$-4x^3$								
$-5x$	$-5x^3$	$+20x$								
$+12$	$12x^2$	$-48$								
<p><b>Dividing Polynomials</b> -Rewrite as separate fractions -Divide the Coefficients -Subtract the exponents</p>	<p>9) <math>\frac{24x^3y^3}{8x^2y^2} - \frac{16x^5y}{8x^2y^2} + \frac{8x^2y^2}{8x^2y^2}</math> <math>3xy - \frac{2x^3}{y} + 1</math></p>									

<p><b>Compositions</b></p> <p>-The right or inside function comes FIRST</p> <p>-Replace x with either the function or number (if given)</p>	<p>10) If <math>f(x) = 2x - 1</math> and <math>g(x) = x^2</math> find <math>(g \circ f)(-2)</math></p> <p><math>f(-2) = 2(-2) - 1 = -5</math></p> <p><math>g(-5) = (-5)^2 = 25</math></p> <p>11) If <math>m(x) = x^2 - 3</math> and <math>k(x) = 4x - 1</math> find <math>m(k(x))</math></p> <p><math>(4x-1)^2 - 3</math>    <math>4x^2 - 4x - 4x + 1 + 3</math></p> <p><math>(4x-1)(4x-1) - 3</math>    <math>4x^2 - 8x + 4</math></p>
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\*\*Answer Key Available at [www.ms-schmidt.weebly.com](http://www.ms-schmidt.weebly.com) Under Notes- Unit 1 Polynomial Expressions

Part I: Simplify each

1)  $5x^2(x^2 + 2x - 4) - 2x^3$

$5x^4 + 2x^3 - 20x^2 - 2x^3$

$5x^4 - 20x^2$

2)  $6 - 4(x + 7)$

$6 - 4x - 28$

$-4x - 22$

3)  $4a - 2[a - 9(2a + 5) + 2a]$

$4a - 2[a - 18a - 45 + 2a]$  →  $4a + 30a + 90$

$4a - 2[-15a - 45]$  →  $34a + 90$

4)  $2y^2 + \frac{1}{3}y(9y - 3) + 8y$

$2y^2 + 3y^2 - y + 8y$

$5y^2 + 7y$

5)  $-3x + \frac{2}{3}(6x - 18) + 5$

$-3x + 4x - 12 + 5$

$x - 7$

6)  $3b - 2\{b^2 - [4b - 9(b + 2)] + 3b^2\}$

$3b - 2\{b^2 - [4b - 9b - 18] + 3b^2\}$

$3b - 2\{b^2 - [-5b - 18] + 3b^2\}$

$3b - 2\{b^2 + 5b + 18 + 3b^2\}$

$3b - 2\{5b + 18 + 4b^2\}$

$3b - 10b - 36 - 8b^2$

$-8b^2 - 7b - 36$

Part II: Evaluate each

7) If  $x = -6$ , find the value of  $2x^2 + \frac{5}{2}x - 1$ .

$$\begin{aligned} & 2(-6)^2 + \frac{5}{2}(-6) - 1 \\ & 2(36) + -15 - 1 \\ & 72 + -15 - 1 = \boxed{56} \end{aligned}$$

8) Evaluate  $-a^2 - (4a + 5) + 2$  when  $a = 4$ .

$$\begin{aligned} & -(4)^2 - (4(4) + 5) + 2 \\ & -16 - (16 + 5) + 2 \\ & -16 - 21 + 2 = \boxed{-35} \end{aligned}$$

9) If  $x = -2$ , and  $y = 5$ , find the value of  $\frac{3x^2 - 2y}{-2xy + 7}$

$$\frac{3(-2)^2 - 2(5)}{-2(-2)(5) + 7} = \boxed{\frac{2}{27}}$$

10) Evaluate  $6 - 2a - 2b^2$ , when  $a = 3$  and  $b = 4$ .

$$\begin{aligned} & 6 - 2(3) - 2(4)^2 \\ & 6 - 6 - 32 = \boxed{-32} \end{aligned}$$

11) Given  $f(x) = 14x^2 - 25$ , evaluate  $f(-2)$

$$\begin{aligned} & 14(-2)^2 - 25 \\ & 14(4) - 25 = \boxed{31} \end{aligned}$$

12) If  $g(y) = 3y^2 - 10y + 5$ , find  $g(4)$

$$\begin{aligned} & 3(4)^2 - 10(4) + 5 = \boxed{13} \\ & 3(16) - 40 + 5 \end{aligned}$$

Part III: Perform the indicated operation

13) From  $3x^2 - 5x + 2$  subtract  $4x^2 - 10$

$$\begin{aligned} & (3x^2 - 5x + 2) + (-4x^2 + 10) \\ & -x^2 - 5x + 12 \end{aligned}$$

14) Add  $(10x^3 + 8x^2 + 1)$  and  $(-7x^3 + 3x^2 - 2x - 1)$

$$3x^3 + 11x^2 - 2x$$

15) Subtract  $(-x^2 + 7x - 3)$  from  $(2x^2 + 7x + 10)$

$$\begin{array}{r} (2x^2 + 7x + 10) + (-x^2 - 7x + 3) \\ \hline 3x^2 + 13 \end{array}$$

16) Simplify:  $(-3a^3 + 5a^2 + a - 13) + (4a^3 + 2a^2 - 6a + 2)$

$$-7a^3 + 7a^2 - 5a - 11$$

17) Multiply:  $(-2x + 3)(6x + 1)$

$$\begin{array}{r} -12x^2 - 2x + 18x + 3 \\ \hline -12x^2 + 16x + 3 \end{array}$$

18) Multiply:  $(3x - 4)(2x^2 + 6x + 9)$

	$2x^2$	$+ 6x$	$+ 9$
$3x$	$6x^3$	$18x^2$	$+ 27x$
$-4$	$-8x^2$	$-24x$	$-36$

$$6x^3 + 10x^2 + 3x - 36$$

19) Simplify:  $2 - 3x(x + 5)^2$

$$\begin{array}{l} 2 - 3x(x + 5)(x + 5) \\ 2 - 3x(x^2 + 5x + 5x + 25) \\ 2 - 3x(x^2 + 10x + 25) \end{array} \rightarrow \begin{array}{l} 2 - 3x^3 - 30x^2 - 75x \\ -3x^3 - 30x^2 - 75x + 2 \end{array}$$

20) Multiply:  $(6x - 7y)^2$

$$\begin{array}{r} (6x - 7y)(6x - 7y) \\ \hline 36x^2 - 42xy - 42xy + 49y^2 \\ \hline 36x^2 - 84xy + 49y^2 \end{array}$$

21) Simplify:  $2 - 5(3x + 2)(x - 4) + 10x$

$$\begin{array}{l} 2 - 5(3x^2 - 4x + 2x + 8) + 10x \\ 2 - 5(3x^2 - 2x + 8) + 10x \\ 2 - 15x^2 + 10x - 40 + 10x \end{array} \rightarrow -15x^2 + 20x - 38$$

22) Simplify:  $\frac{36x^2y}{12xy^3}$

$$\frac{3x}{y^2}$$

23) Divide:  $\frac{27x^3 + 9x^2 - 3x}{3x}$

$$\frac{27x^3}{3x} + \frac{9x^2}{3x} - \frac{3x}{3x}$$

$$3x^2 + 3x - 1$$

24) Divide:  $\frac{28a^4b^2 - 12a^3b + 2a^2b^3}{4a^2b}$

$$\frac{28a^4b^2}{4a^2b} - \frac{12a^3b}{4a^2b} + \frac{2a^2b^3}{4a^2b}$$

$$7a^2b - 3a + \frac{b^2}{2}$$

25) Divide:  $\frac{100y^3 + 35yz - 10z^2}{5yz}$

$$\frac{100y^3}{5yz} + \frac{35yz}{5yz} - \frac{10z^2}{5yz}$$

$$\frac{20y^2}{z} + 7 - \frac{2z}{y}$$

26) Divide:  $\frac{16x^2y + 12xy^2}{4xy}$

$$\frac{16x^2y}{4xy} + \frac{12xy^2}{4xy}$$

$$4x + 3y$$

Part IV: Compositions

27) Given  $f(x) = 3x - 2$  and  $g(x) = x^2 - 3$  find  $(g \circ f)(2)$

$$f(2) = 3(2) - 2 = 4$$

$$g(4) = (4)^2 - 3 = 13$$

28) If  $f(x) = 2x - 1$  and  $h(x) = x^2 + 1$ , find  $(h \circ f)(-4)$

$$f(-4) = 2(-4) - 1 = -9$$

$$h(-9) = (-9)^2 + 1 = 82$$

29) Given  $f(x) = 2x - 1$  and  $g(x) = 2x^2 - 3x$  find  $g(f(x))$

$$2(2x-1)^2 - 3(2x-1)$$

$$2(4x^2 - 2x - 2x + 1) - 3(2x-1)$$

$$2(4x^2 - 4x + 1) - 3(2x-1)$$

$$8x^2 - 8x + 2 - 6x + 3$$

$$8x^2 - 14x + 5$$

30) If  $f(x) = x^2 - 1$  and  $g(x) = 2x + 5$ , find  $f(g(x))$

$$(2x+5)^2 - 1$$

$$(2x+5)(2x+5) - 1$$

$$4x^2 + 10x + 10x + 25 - 1$$

$$4x^2 + 20x + 24$$