

Lesson 1.6 Objective: SWBAT determine the key features of a polynomial function.

Kickoff

Find the average rate of change of the function,  $f(x) = x^2 - x$  between the values  $x = -1$  and  $x = 3$ .

$$\begin{matrix} (-1, 2) & (3, 6) \\ x_1 & y_1 & x_2 & y_2 \end{matrix}$$

$$\frac{\Delta y}{\Delta x} = \frac{6-2}{3-(-1)} = \frac{4}{4} \quad m = 1$$

Key Features of Polynomials

- Increasing
- Decreasing
- Zeros
- Relative minimum and maximum
- Symmetry

Increasing/Decreasing-

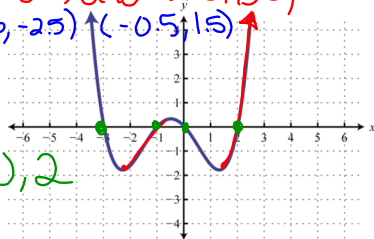
↳ up    ↳ down    intervals using x-values

Increasing:  $(-2.5, -0.5)$  and  $(1.5, \infty)$

Decreasing:  $(-\infty, -2.5)$  and  $(-0.5, 1.5)$

Zeros - roots / x-intercepts

$x = -3, -1, 0, 2$



Relative Minimum - Smallest pt inside the graph

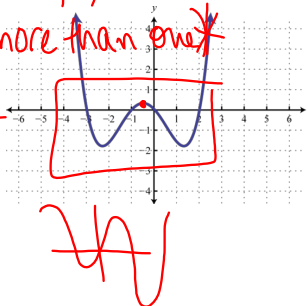
$(-2.5, -2)$  and  $(1.5, -2)$

\*there can be more than one\*

Relative Maximum -

highest pt inside the graph:

$(-0.5, 0.5)$



Symmetry

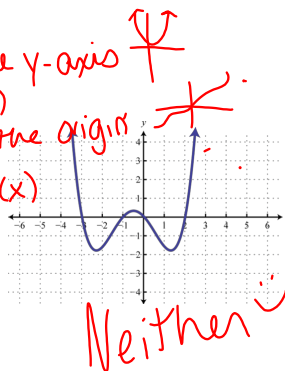
Even - Symmetric to the y-axis

Algebraic =  $f(x) = f(-x)$

Odd - Symmetric to the origin

Algebraic =  $f(x) = -f(-x)$

Neither - not odd or even.



Symmetry Algebraically

1.  $k(x) = \frac{x}{x^2+1}$

$$k(-x) = \frac{-x}{(-x)^2+1} = \frac{-x}{x^2+1} = -\left(\frac{x}{x^2+1}\right)$$

Odd

2.  $m(x) = x^4 - |x|$

$$m(-x) = (-x)^4 - |(-x)| = x^4 - |x|$$

Even

3.  $t(x) = x + 6$   
 $t(-x) = (-x) + 6 = -x + 6$

Neither

Key Features	
End Behavior	<del>Degree is _____</del> <del>Leading Coefficient is _____</del>
Domain	
Range	
Increasing	
Decreasing	
Roots	
x-intercept(s)	
y-intercept(s)	
Relative Maximum(s)	
Relative Minimum(s)	
Odd/Even/Neither	

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