

Lesson 1.9 Objective: SWBAT perform operations with polynomials.

Kickoff

1) Using your graphing calculator, find the relative maximums, relative minimums, zeros, increasing and decreasing for the function: $f(x) = x^3 - 5x + 1$

Three Decimal places

min: $(-1.28, -3.30)$ increasing: $(-\infty, -1.28)$ $(1.28, \infty)$
 max: $(1.28, 5.30)$ decreasing: $(-1.28, 1.28)$
 $.0.202, 2.128, -2.330$

Describe in words each transformation in the correct order.

- 1) $f(x-1)+5$ ① right 1 ② up 5
 2) $2g(x-1)$ ② Narrower/Stretch ① right 1
 3) $-3g(x)-7$ ① Reflection over x-axis ② Narrower/Stretch ③ Down 7
 4) $-\frac{1}{2}h(x-4)+1$ ② Reflection over x-axis ③ wider/Shrink ① right 4 ④ up 1
 5) $10g(x-5)-7$ ② Narrower/Stretch ① Right 5 ③ Down 7
 6) $-h(x+2)+3$ ② Reflection over x-axis ① left 2 ③ up 3

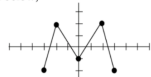
Write each description using function notation.

- 7) A reflection over the x axis and a shift left 2 $-f(x+2)$
 8) A vertical stretch of $\frac{1}{2}$ and a shift up 7 $\frac{1}{2}f(x)+7$
 9) A vertical stretch of 3, a reflection over the x-axis, and a shift down 3 $-3f(x)-3$
 10) A reflection over the x-axis, a vertical stretch of $\frac{3}{4}$ and a shift up 1 and right 1 $-\frac{3}{4}f(x-1)+1$

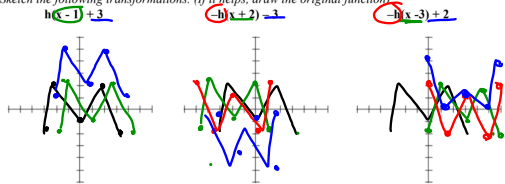
Write each description using the function given.

- 11) A quadratic function with a vertical stretch of 4, a shift up 2 and right 7 $f(x) = 4(x-7)^2 + 2$
 12) A cubic function that has a horizontal shift right 3 and then reflects over the x-axis and then shifts down 4 units. $f(x) = -(x-3)^3 - 4$
 13) A square root function that has a horizontal shift left 2 and then reflects over the y-axis and then shifts up 6 units. $f(x) = \sqrt{-(x+2)} + 6$
 14) An absolute value function that has a horizontal shift right 1 and then reflects over the x-axis, has a vertical stretch of 4 and then then shifts down 7 units. $f(x) = -4|x-1|-7$

15) Using the graph of $h(x)$ pictured below,



Sketch the following transformations. (If it helps, draw the original function)



Fill in the missing parts to the chart.

Equation	Parent Function	Description of shifts	New Vertex/Point
$f(x) = x-3 +1$	Absolute value	right 3 up 1	(3, 1)
$g(x) = -(x+6)^2 - 2$	Quadratic	Reflection over x left 6 / down 2	(-6, -2)
$h(x) = 2\sqrt{-x} + 5$	Square root	Narrower / up 5 Reflect over y	(0, 5)
$j(x) = -3(x-4)^2 + 9$	Cubic	Reflect over x Stretch 3 Shift 4 / up 9	(4, 9)
$f(x) = \frac{1}{2}(x+2)^2$	Quadratic	wider left 2	(-2, 0)
$f(x) = 4 x-10 -7$	Absolute value	right 10 Narrower down 7	(10, -7)
$h(x) = 2\sqrt{x-9} + 5$ $\sqrt{-(x+9)}$	Square root	Narrower reflection over y up 5 left 9	(9, 5)

Adding & Subtracting Polynomials

Combine like terms! →

1) $(9r^3 + 5r^2 + 11r) + (-2r^3 + 9r - 8r^2)$
 $7r^3 - 3r^2 + 20r$

2) $(3a^2 + 2a - 2) + (a^2 + 3a - 7)$
 $2a^2 + 5a - 9$

① Keep 1st poly.
 ② change +
 ③ change 2nd signs

Multiplying Polynomials

3) $(8a - 3b)(2a - 9b)$

① multiply coeff. $2a \begin{array}{|c|c|} \hline 8a & -3b \\ \hline \end{array}$

② add exponents $16a^2 - 78ab + 27b^2$

③ Combine!

4) $(2x^2 + 7x)^2$
 $(2x^2 + 7x)(2x^2 + 7x)$
 $4x^4 + 14x^3 + 14x^3 + 49x^2$
 $4x^4 + 28x^3 + 49x^2$

Dividing Polynomials

① divide coeff.
 ② Subtract exponents

5) $\frac{18a^2g + 27a^2g^2 - 9ag^2}{9a^2g}$
 $2 + 3g - \frac{1g}{a}$

6) $\frac{25x^2y^2 + 35xy^3 + 50x^3y^2}{-5xy}$
 $-5xy - 7y^2 - 10x^2y$

$a^{-1} = \frac{1}{a}$
 $a^{-3} = \frac{1}{a^3}$

Worksheet

11) $f(t) = -4t + 4$
 $h(t) = t^2 + 2t$
 Find $f(n^2) - h(n^2)$

$(-4(n^2) + 4) + (-(n^2)^2 - 2(n^2))$
 $-4n^2 + 4 + -n^4 - 2n^2$
 $-n^4 - 6n^2 + 4$

Find your partner from yesterday, complete at least the front page of the worksheet!