

Lesson 34- Objective: SWBAT solve polynomial functions with mixed roots.

Kickoff- Solve the following quadratic equations in simplest radical form.

1) $-2x^2 + 4x + 6 = 15$
 $-2x^2 + 4x - 9 = 0$
 $a = -2, b = 4, c = -9$
 $x = \frac{-4 \pm \sqrt{4^2 - 4(-2)(-9)}}{2(-2)}$
 $x = \frac{-4 \pm \sqrt{16 - 72}}{-4}$
 $x = \frac{-4 \pm \sqrt{-56}}{-4}$
 $x = \frac{-4 \pm 2i\sqrt{14}}{-4}$
 $x = \frac{-1 \pm i\sqrt{14}}{-1}$
 $x = 1 \pm i\sqrt{14}$

2) $5x^2 - 5x + 2 = 3x(x - 1)$
 $5x^2 - 5x + 2 = 3x^2 - 3x$
 $2x^2 - 2x + 2 = 0$
 $x^2 - x + 1 = 0$
 $x^2 - x + \frac{1}{4} = -1 + \frac{1}{4}$
 $\sqrt{(x - \frac{1}{2})^2} = \sqrt{-\frac{3}{4}}$
 $x - \frac{1}{2} = \pm i\frac{\sqrt{3}}{2}$
 $x = \frac{1}{2} \pm i\frac{\sqrt{3}}{2}$

7) $\frac{3}{2} \pm \frac{i\sqrt{5}}{2}$

8) $\frac{6}{7} \pm \frac{i\sqrt{31}}{7}$

9) $-\frac{4}{5} \pm \frac{3i}{5}$

10) $x = 0$
 $x = -\frac{4}{13}$
 $13x^2 + 4x = 0$
 $x(13x + 4) = 0$
 $x = 0 \quad 13x + 4 = 0$

Solving Polynomial Functions with Mixed Roots

Try This: Find all possible rational zeros.

$f(x) = 3x^3 - 4x^2 + x + 15$

$\pm 15, \pm 5, \pm 3, \pm 1$

$\pm 3, \pm 1$

$\pm 15, \pm 5, \pm 3, \pm 1, \pm \frac{5}{3}, \pm \frac{1}{3}$

Solving Polynomial Functions with Mixed Roots

- 1) Find the possible rational zeros
- 2) Use calculator to find a possible zero.
- 3) Use the Factor Theorem to find the zero.
- 4) Synthetically Divide to break down the polynomial function
- 5) Keep doing these steps until you have a quadratic!
- 6) Once you get a quadratic solve using: Quadratic Formula, Factoring/DOTS, Complete the Square

Directions: Find the zeros of the polynomial function.

Ex1: $f(x) = x^3 - 8x^2 - 51x - 62$

Possible Zeros: $\pm 62, \pm 31, \pm 2, \pm 1$

$f(-2) = 0$

$f(x) = (x+2)(x^2 - 10x - 31) = 0$

$x+2=0 \Rightarrow x=-2$

$x^2 - 10x - 31 = 0$
 $x = \frac{10 \pm \sqrt{10^2 - 4(1)(-31)}}{2}$
 $x = \frac{10 \pm \sqrt{100 + 124}}{2}$
 $x = \frac{10 \pm \sqrt{224}}{2}$
 $x = \frac{10 \pm 2\sqrt{56}}{2}$
 $x = 5 \pm \sqrt{14}$

Zeros: $\{-2, 5 + \sqrt{14}, 5 - \sqrt{14}\}$

Ex2: $f(x) = 9x^4 + 9x^3 + 18x^2 - 90x - 108$

Possible Zeros: $\pm 108, \pm 54, \pm 36, \pm 27, \pm 18, \pm 12, \pm 9, \pm 6, \pm 4, \pm 3, \pm 2, \pm 1$

$\pm 9, \pm 3, \pm 1$

Possible Zeros: $\pm 108, \pm 54, \pm 36, \pm 27, \pm 18, \pm 12, \pm 9, \pm 6, \pm 4, \pm 3, \pm 2, \pm 1, \pm \frac{4}{3}, \pm \frac{2}{3}, \pm \frac{1}{3}, \pm \frac{1}{9}, \pm \frac{1}{27}$

$f(-1) = 0$

$f(x) = (x+1)(x-2)(9x^2 + 18x + 54) = 0$

$x = -1, x = 2$

Zeros: $x^2 + 2x + 6 = 0$
 $x = \frac{-2 \pm \sqrt{2^2 - 4(1)(6)}}{2}$
 $x = \frac{-2 \pm \sqrt{4 - 24}}{2}$
 $x = \frac{-2 \pm \sqrt{-20}}{2}$
 $x = \frac{-2 \pm 2i\sqrt{5}}{2}$
 $x = -1 \pm i\sqrt{5}$

Practice:

1) $f(x) = x^4 - 16$

2) $h(x) = x^4 - x^3 - 9x^2 - 3x - 36$

3) $g(x) = x^4 - 4x^3 + 8x^2 - 8x$

4) $j(x) = x^4 - 6x^3 - 11x^2 + 86x - 120$

5) $f(x) = x^5 - 8x^4 + 87x^3 - 284x^2 + 268x$