

Lesson 48 Objective: SWBAT solve rational equations.

Kickoff

Place your weekly HW quiz on the desk and take the lesson paper!

Complete the try this!

Rational Equations

Try This: Solve for x

$$\text{1) } \frac{x+2}{x-2} = \frac{2}{3}$$

$$\begin{aligned} 3(x+2) &= 2(x-2) \\ 3x+6 &= 2x-4 \\ -3x &\quad -3x \\ 6 &= -x \\ 9 &= x \end{aligned}$$

$$\text{2) } \frac{x}{x+3} = \frac{8}{x+6}$$

$$\begin{aligned} 8(x+3) &= x(x+6) \\ 8x+24 &= x^2+6x \\ 0 &= x^2-2x-24 \\ 0 &= (x-6)(x+4) \\ x &= 6 \quad x = -4 \end{aligned}$$

Fractional Equations-

- 1) Find the LCD. (both sides)
- 2) Multiply numerators by LCD.
- 3) Simplify !!
- 4) Solve!
- *5) Check for extraneous roots!

Examples:

$$\text{1) } \frac{4x}{x} + \frac{1}{6} = \frac{1}{2}$$

$$\begin{aligned} \cancel{\frac{4x}{x}} + \cancel{\frac{1}{6}} &= \frac{1}{2} \\ 6 + x &= 3x \\ -x &\quad -x \\ 6 &= 2x \\ 3 &= x \end{aligned}$$

Check

$$\begin{aligned} \frac{1}{x} + \frac{1}{6} &= \frac{1}{2} \\ \frac{1}{3} + \frac{1}{6} &= \frac{1}{2} \\ \frac{1}{2} &= \frac{1}{2} \checkmark \end{aligned}$$

$$\text{2) } \frac{x(x-1)}{x-1} = \frac{2}{x} + \frac{1}{x-1}$$

$$\begin{aligned} x^2 &= 2(x-1) + x \\ x^2 &= 2x-2+x \\ x^2 &= 3x-2 \\ -3x+2 &\quad -3x+2 \\ x^2-3x+2 &= 0 \\ (x-2)(x-1) &= 0 \\ x = 2 & \quad \cancel{x=1} \end{aligned}$$

$$\text{3) } \frac{(x-2)(x+3)}{x-2} - \frac{8(x-2)}{x+3} = \frac{10(x+3)}{x^2+2x-6}$$

$$x(x+3) - 8(x-2) = 10$$

$$x^2+3x-8x+16 = 10$$

$$x^2-5x+16 = 10$$

$$x^2-5x+6 = 0$$

$$(x-3)(x-2) = 0$$

$$x = 3 \quad \cancel{x=2}$$

Solve each equation. Remember to check for extraneous solutions.

$$1) \frac{1}{5x^2} - \frac{x+5}{x^2} = \frac{1}{x}$$

$$2) \frac{3}{2} = \frac{b+5}{4b} + \frac{3}{2b}$$

$$3) \frac{1}{a+2} + \frac{6a+4}{a^2-3a-10} = \frac{1}{a-5}$$

$$4) \frac{1}{k-3} = \frac{3}{k-3} + \frac{2}{k+4}$$