

Kick off-

1) Simplify the following radicals.

a)  $\sqrt{28}$   
 $\frac{1}{4}\sqrt{7} \cdot 2\sqrt{7}$

b)  $3\sqrt{72}$   
 $\frac{\sqrt{36}}{3} \cdot \sqrt{2}$   
 $(\cancel{18})\sqrt{2}$

Perfect Squares: 4, 9, 16, 25, 36, 49, 64, 81, 100

2) Find the inverse ( $f^{-1}(x)$ ) of  $\frac{x-2}{3} = f(x)$

$\frac{x-2}{3} = f'(x)$   
 $x-2 = 3f'(x)$   
 $x-2 = 3y+2$   
 $\underline{x-2 = 3y+2}$

$\frac{x-2}{3} = f'(x)$   
 $y = \frac{1}{3}x - 8$   
 $x = 3y + 8$   
 $+8$   
 $\underline{x+8 = 3y+16}$   
 $y = \frac{1}{3}x + 16$

$\frac{x-2}{3} = f'(x)$   
 $\frac{1}{3}x + 8 = \frac{1}{3}y (\cancel{\frac{1}{3}})$   
 $2x + 16 = y$   
 $2x + 16 = f^{-1}(x)$

- ⑦ 8  
⑧  $\frac{3}{5}x - \frac{6}{5} = f^{-1}(x)$   
⑨  $8\sqrt{2}$   
⑩  $\frac{x-1}{6} = f^{-1}(x)$   
⑪  $\frac{x-7}{4} = f^{-1}(x)$   
⑫  $15\sqrt{2}$   
⑬  $-3x - 15 = f^{-1}(x)$   
⑭  $10\sqrt{10}$   
⑮ 12  
⑯  $\frac{x-6}{-2} = f^{-1}(x)$   
⑰  $15\sqrt{5}$   
⑱  $5\sqrt{5}$   
⑲  $40\sqrt{2}$   
⑳  $x^2 - 46$

Perfect Squares involving variables

1)  $\sqrt{x^2}$   
 $x^1$  or  $x$

2)  $\sqrt{x^4}$   
 $x^2$

3)  $\sqrt{x^6}$   
 $x^3$

4)  $\sqrt{x^8}$   
 $x^4$

\*Rule- divide the even exponents by 2.

To Simplify a Radical Expression

- Find the factors of the inside number and one of the factors must be a perfect square.
- Split the inside numbers into two different radicals
- The perfect square, and the highest even exponent variable first and then the other factor and any odd exponent variables.
- Take the square root of the perfect square and divide the variables exponent by 2 and if there is a number on the outside multiply it to the number.

Examples: Put each of the following in simplest radical form.

1)  $\sqrt{144}$   
 $\sqrt{4} \times \sqrt{36}$   
 $2 \cdot 6$   
 $\boxed{3 \cdot 4}$   
 $2 \times \sqrt{3}$

2)  $\sqrt{8x^6}$   
 $\sqrt{4x^6} \times \sqrt{2}$   
 $\boxed{2 \cdot 4}$   
 $\sqrt{4} \times \sqrt{2}$   
 $2 \times \sqrt{2}$

3)  $\sqrt{2x^7y^6}$   
 $\sqrt{4x^6} \times \sqrt{2xy}$   
 $\boxed{2 \cdot 4}$   
 $2 \times \sqrt{2xy}$

4)  $\sqrt{72x^7y^6}$   
 $\sqrt{36x^6} \times \sqrt{2xy}$   
 $\boxed{4 \cdot 9}$   
 $4 \times \sqrt{2xy}$

5)  $\sqrt{63x^2y^6}$   
 $\sqrt{9x^2} \times \sqrt{7y^6}$   
 $\boxed{3 \cdot 7}$   
 $3xy^3\sqrt{7}$

6)  $\sqrt{32x^3y^9}$   
 $\sqrt{16x^2} \times \sqrt{2xy}$   
 $\boxed{4 \cdot 9}$   
 $4x^2y^4\sqrt{2xy}$

3)  $\sqrt{27x^3}$   
 $\sqrt{9x^2} \times \sqrt{3x}$   
 $\boxed{9 \cdot 3}$   
 $3x\sqrt{3x}$

4)  $\sqrt[3]{18y^5}$   
 $\sqrt[3]{2 \cdot 9y^5}$   
 $\boxed{2 \cdot 9y^4}$   
 $\sqrt[3]{9} \times \sqrt[3]{y^4} \times \sqrt[3]{2y}$   
 $\boxed{3 \cdot 3y^2}$   
 $-3 \cdot 3y^2\sqrt[3]{2y}$   
 $-9y^2\sqrt[3]{2y}$

5)  $\sqrt{63x^2y^6}$   
 $\sqrt{9x^2} \times \sqrt{7y^6}$   
 $\boxed{9 \cdot 7}$   
 $3xy^3\sqrt{7}$

7)  $\sqrt{72x^7y^6}$   
 $\sqrt{36x^6} \times \sqrt{2xy}$   
 $\boxed{4 \cdot 9}$   
 $4x^3y^3\sqrt{2xy}$

8)  $\sqrt{975x^3y^7}$   
 $\sqrt{25x^2} \times \sqrt{3xy^7}$   
 $\boxed{25 \cdot 3}$   
 $5x\sqrt{3}x^2y^7$

9)  $\sqrt{32x^3y^9}$   
 $\sqrt{16x^2} \times \sqrt{2xy}$   
 $\boxed{16 \cdot 9}$   
 $4x^2y^4\sqrt{2xy}$

9)  $2\sqrt{50x^5y^7}$

$$\begin{aligned} &\cancel{\sqrt{25x^4y^6}} \cdot \sqrt{2xy} \\ &\rightarrow 5x^2y^3 \sqrt{2xy} \\ &10x^2y^3\sqrt{2xy} \end{aligned}$$

$\sqrt{1x^2y^4z^8}\sqrt{1xyz}$

$$\begin{aligned} &\cancel{\sqrt{x^2y^2z^4}} \cdot \sqrt{xyz} \\ &\rightarrow xy^2z^4\sqrt{xyz} \end{aligned}$$

10)  $\sqrt{18x^{10}y^8}$

$$\begin{aligned} &\cancel{\sqrt{9x^8y^8}} \cdot \sqrt{2} \\ &\rightarrow 3x^5y^4\sqrt{2} \end{aligned}$$

11)  $\sqrt{x^3y^5z^9}$

$$\begin{aligned} &\cancel{\sqrt{9x^4y^6z^3}} \cdot \sqrt{5xz} \\ &\rightarrow 3x^3y^3z\sqrt{5xz} \\ &6x^2y^3z\sqrt{5xz} \end{aligned}$$