

Lesson 67 Objective: SWBAT use the unit circle to find the terminal angle.

Kickoff

1) If  $\theta$  in standard position is  $\frac{5\pi}{6}$  find the coordinate of the point that intersects the unit circle.  
 2) If  $\theta$  is an angle in standard position and intersects the unit circle at P. Find all six trigonometric functions.  $P(-\frac{\sqrt{3}}{2}, -\frac{1}{2})$

①  $\cos \frac{5\pi}{6} = -\frac{\sqrt{3}}{2}, \sin \frac{5\pi}{6} = \frac{1}{2}$   
 $(-\frac{\sqrt{3}}{2}, \frac{1}{2})$

②  $\cos \theta = -\frac{\sqrt{3}}{2}$   
 $\sin \theta = -\frac{1}{2}$   
 $\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{-\frac{1}{2}}{-\frac{\sqrt{3}}{2}} = \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}$   
 $\csc \theta = -\frac{1}{\sin \theta} = -2$   
 $\sec \theta = \frac{1}{\cos \theta} = -\frac{2}{\sqrt{3}} = -\frac{2\sqrt{3}}{3}$   
 $\cot \theta = \frac{1}{\tan \theta} = \sqrt{3}$

Unit Circle Day 2

Try This: Draw the unit circle and label the points on the axes

$\sin \theta = y$   
 $\cos \theta = x$   
 $\tan \theta = \frac{y}{x} = \frac{\sin \theta}{\cos \theta}$   
 $P(x,y) = (\cos \theta, \sin \theta)$

Quadrant Angles: Fill in the chart using the unit circle above.

$\theta$	$0^\circ, 360^\circ$ $0, 2\pi$	$90^\circ$ $\frac{\pi}{2}$	$180^\circ$ $\pi$	$270^\circ$ $\frac{3\pi}{2}$
$\sin \theta$	0	1	0	-1
$\cos \theta$	1	0	-1	0
$\tan \theta$	0	DNE	0	DNE

\*  $90^\circ$  is  $\frac{\pi}{2}$  in rad.

Trig Functions in the Quadrants:

II (-, +) I (+, +)  
 III (-, -) IV (+, -)

How To Remember:

S	A
T	C

All students take calc.

Determine which quadrant that  $\theta$  lies in.

- $\sin \theta > 0, \cos \theta < 0$  II
- $\tan \theta < 0, \cos \theta > 0$  IV
- $\cos \theta > 0, \tan \theta > 0$  I
- $\sin \theta < 0, \cos \theta < 0$  III
- $\csc \theta > 0, \cos \theta < 0$  III
- $\cot \theta > 0, \sec \theta < 0$  III
- $\sin \theta < 0, \cot \theta > 0$  III

Cofunctions:

$\beta + \theta = 90$   
 $\sin \beta = \frac{4}{5}$   
 $\cos \theta = \frac{4}{5}$

\*  $\theta$ 's add  $90^\circ$  and are =

Trig Function	Cofunction
$\sin \theta$	$\cos \theta$
$\sec \theta$	$\csc \theta$
$\tan \theta$	$\cot \theta$

Ex:  $\cot(x - 10) = \tan(4x)$   
 $x - 10 + 4x = 90$   
 $5x - 10 = 90$   
 $5x = 100$   
 $x = 20$

$\frac{1}{\tan}$