

Lesson 67 Objective: SWBAT use the unit circle to find the terminal angle.

## Kickoff

1) If  $\theta$  in standard position is  $\frac{5\pi}{6}$  find the coordinate of the point that intersects the unit circle.

2) If  $\theta$  is an angle in standard position and intersects the unit circle at P. Find all six trigonometric functions.  $P(\frac{-\sqrt{3}}{2}, \frac{1}{2})$

$$\textcircled{1} \quad (\cos \frac{5\pi}{6} = -\frac{\sqrt{3}}{2}, \sin \frac{5\pi}{6} = \frac{1}{2}) \quad (-\frac{\sqrt{3}}{2}, \frac{1}{2})$$

$$\textcircled{2} \quad \cos \theta = -\frac{\sqrt{3}}{2}$$

$$\sin \theta = -\frac{1}{2}$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{-\frac{1}{2}}{-\frac{\sqrt{3}}{2}} \rightarrow \frac{1}{2} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \frac{1}{2}$$

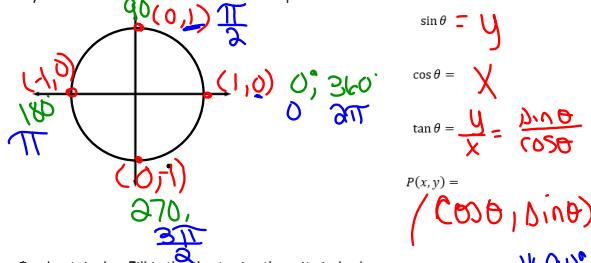
$$\sec \theta = -\frac{2}{\sqrt{3}} = -\frac{2\sqrt{3}}{3}$$

$$\csc \theta = -\frac{\sqrt{3}}{2} = -\frac{2\sqrt{3}}{3}$$

$$\cot \theta = \frac{\sqrt{3}}{1} = \sqrt{3}$$

## Unit Circle Day 2

Try This: Draw the unit circle and label the points on the axes



$$\sin \theta = y$$

$$\cos \theta = x$$

$$\tan \theta = \frac{y}{x} = \frac{\sin \theta}{\cos \theta}$$

$$P(x, y) = (\cos \theta, \sin \theta)$$

\*90° is  $\frac{\pi}{2}$  in rad

Quadrant Angles: Fill in the chart using the unit circle above.

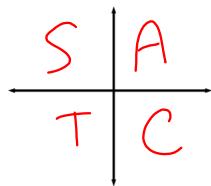
$\theta$	$0^\circ, 360^\circ$ 0, $2\pi$	$90^\circ$ $\frac{\pi}{2}$	$180^\circ$ $\pi$	$270^\circ$ $\frac{3\pi}{2}$
$\sin \theta$	0	1	0	-1
$\cos \theta$	1	0	-1	0
$\tan \theta$	0	DNE	0	DNE

Trig Functions in the Quadrants:

- II (-, +) I (+, +)
- + sine, cosine, secant, cosecant
- tangent, cotangent, tangent, cotangent
- cosine, secant, cosecant, tangent
- sine, cosine, secant, cosecant
- + tangent, cotangent, tangent, cotangent

III (-, -) IV (+, -)

How To Remember:



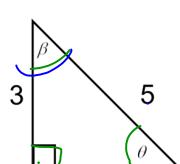
All Students take Calc.

Determine which quadrant that  $\theta$  lies in.

- 1)  $\sin \theta > 0, \cos \theta < 0$  II
- 2)  $\tan \theta < 0, \cos \theta > 0$  IV
- 3)  $\cos \theta > 0, \tan \theta > 0$  I
- 4)  $\sin \theta < 0, \cos \theta < 0$  III
- 5)  $\csc \theta > 0, \cos \theta < 0$  III
- 6)  $\cot \theta > 0, \sec \theta < 0$  II
- 7)  $\sin \theta < 0, \cot \theta > 0$  IV



## Cofunctions:



$$\beta + \theta = 90^\circ$$

$$\sin \beta = \frac{4}{5}$$

$$\cos \theta = \frac{4}{5}$$

4. \*if's add  $90^\circ$  and are =

Trig Function	Cofunction
$\sin \theta$	$\cos \theta$
$\sec \theta$	$\csc \theta$
$\tan \theta$	$\cot \theta$

$$\text{Ex: } \cot x - 10 = \tan(4x)$$

$$X - 10 + 4x = 0$$

$$5x - 10 = 0$$

$$5x = 10$$

$$X = 20$$