

Lesson 7.8- Solving Quadratic Equations by Completing the square.notebook February 05, 2018

Lesson 7.8: SWBAT solve quadratic equations by completing the square.

Kick off:
Solve each of the following by factoring:

1) $x^2 - x = 12$
 $x^2 - x - 12 = 0$
 $(x-4)(x+3) = 0$
 $x-4=0$ or $x+3=0$
 $x=4$ or $x=-3$

2) $x^2 - 100 = 0$
 $x^2 = 100$
 $x = \pm 10$
 $x = 10$ or $x = -10$

Solve each of the following by quadratic formula:

3) $4x^2 + 4x - 9 = 1$
 $4x^2 + 4x - 10 = 0$
 $a=4$, $b=4$, $c=-10$
 $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
 $\frac{-4 \pm \sqrt{16 - 4(4)(-10)}}{2(4)}$
 $\frac{-4 \pm \sqrt{16 + 160}}{8}$
 $\frac{-4 \pm \sqrt{176}}{8}$
 $\frac{-4 \pm 4\sqrt{11}}{8}$
 $\frac{-1 \pm \sqrt{11}}{2}$

4) $x^2 - 4x - 14 = -2$
 $x^2 - 4x - 12 = 0$
 $a=1$, $b=-4$, $c=-12$
 $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
 $\frac{-(-4) \pm \sqrt{(-4)^2 - 4(1)(-12)}}{2(1)}$
 $\frac{4 \pm \sqrt{16 + 48}}{2}$
 $\frac{4 \pm \sqrt{64}}{2}$
 $\frac{4 \pm 8}{2}$
 $\frac{4+8}{2} = \frac{12}{2} = 6$ or $\frac{4-8}{2} = \frac{-4}{2} = -2$

Solve by completing the square: $x^2 - 4x - 14 = -2$

$x^2 - 4x = 12$

$\left(\frac{1}{2}b\right)^2$ add to both sides
 $(-2)^2 = 4$
 factor

$x^2 - 4x + 4 = 12 + 4$
 $(x-2)(x-2) = 16$
 $\sqrt{(x-2)^2} = \sqrt{16}$
 $x-2 = \pm 4$

$x-2 = 4$ $x-2 = -4$
 $+2 \quad +2$ $+2 \quad +2$
 $x = 6$ $x = -2$

Solve each of the following by completing the square:

1) $x^2 - 5x = -11 + 7x$

2) $x^2 - 5x = -14x$

3) $x^2 = -6x - 8$

4) $k^2 - 12k + 23 = 0$

5) $r^2 - 4r - 91 = 7$

6) $x^2 + 26 = 10x + 8$