

Lesson 94 Objective: SWBAT solve multi-variable systems of equations.

Kickoff
Solve the following by elimination.

$$\begin{array}{r} -4(-7x - 8y = 9) \\ -7(-4x + 9y = -22) \end{array}$$

$$\begin{array}{r} 28x + 32y = -36 \\ + -28x + 63y = -154 \\ \hline 95y = -190 \\ 95 \\ \hline y = -2 \end{array}$$

$(1, -2)$

$$\begin{array}{r} -7x - 8y = 9 \\ -7x - 8(-2) = 9 \\ -7x + 16 = 9 \\ -7x = -7 \\ \hline x = 1 \end{array}$$

Apr 19-6:56 AM

Homework

Apr 19-6:58 AM

Multi-Variable Systems


What is a multi-variable system?

- When you're solving a system of equations with three or more variables, you are solving for the intersection (if any) between three planes.

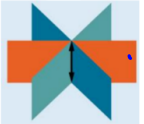
Types of Intersections

Consistent Systems have at least one point of intersection for all three planes

A Point




A Line



Inconsistent Systems do not have any points of intersection for all three planes.

No Intersections



Apr 19-6:55 AM

Steps to Solve Algebraically:

- Pick any **two pairs** of equations from the system.
- Eliminate the same variable from **each pair**. You will have two new equations.
- Use the two equations found in step 2 and create a new system of equations and solve. At this point you will have **solved for one of the variables**.
- Substitute the variable found in step 3 back into one of the two equations from step 2. At this point you will have **solved for another variable**.
- Take the two variables found from steps 3 and 4 and plug them into one of the original equations. At this point you will have found the **last variable**.
- Check by plugging all solutions into all three equations.

Apr 19-6:56 AM

Example 1: Solve the system of equations algebraically for x, y and z.

$$\begin{cases} 4x - 3y + z = -10 \\ 2x + y + 3z = 0 \\ -x + 2y - 5z = 17 \end{cases}$$

$$\begin{array}{r} ① 4x - 3y + z = -10 \\ ② 2(2x + y + 3z = 0) \\ \hline 4x - 3y + z = -10 \\ -4x - 2y - 6z = 0 \\ \hline ③ -5y - 5z = -10 \end{array}$$

$$\begin{array}{r} ③ 2x + y + 3z = 0 \\ ④ (-x + 2y - 5z = 17) \\ \hline 2x + y + 3z = 0 \\ -2x + 4y - 10z = 34 \\ \hline ⑤ 5y - 7z = 34 \end{array}$$

$$\begin{array}{r} ③ -5y - 5z = -10 \\ ⑤ 5y - 7z = 34 \\ \hline -5y + 10 = -10 \\ -5y = -20 \\ \hline y = 4 \end{array}$$

$$\begin{array}{r} -5y - 5z = -10 \\ ⑤ 5y - 7z = 34 \\ \hline -12z = 24 \\ \hline z = -2 \end{array}$$

$$\begin{array}{r} ① 4x - 3y + z = -10 \\ 4x - 3(4) + (-2) = -10 \\ 4x - 12 - 2 = -10 \\ 4x - 14 = -10 \\ 4x = 4 \\ \hline x = 1 \end{array}$$

$(1, 4, -2)$

Apr 19-6:56 AM

Example 2: Solve the system of equations algebraically for x, y and z.

$$\begin{cases} x - 2y + 3z = 7 \\ 2x + y + z = 4 \\ -3x + 2y - 2z = -10 \end{cases}$$

$(2, -1, 1)$

Practice

① $(2, -3, 0)$

Apr 19-6:56 AM

Fix these:

② ① $5a + 6b - 4c = 30$

④ ③ $-4r - 5s - 2t = 4$

⑤ ② $-5a - 6b + 4c = -29$

③ $-2a - 3b - c = -16$

⑥ ③ $6x + 4y - 4z = 8$

Apr 19-1:35 PM