

① Odds only!

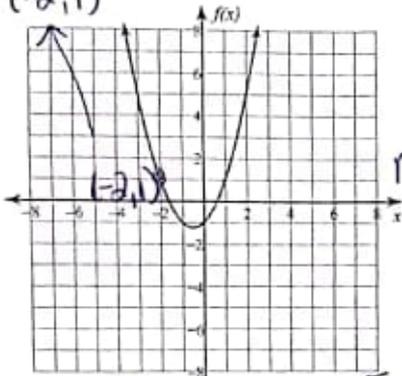
Average Rates of Change - Slope!

Name _____

Date _____ Period _____

For each problem, find the average rate of change of the function over the given interval.

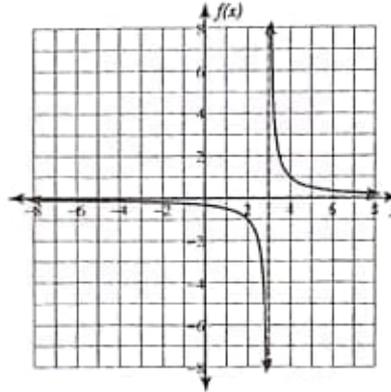
1) $f(x) = x^2 + x - 1$; $[-2, -\frac{7}{4}]$



$$m = \frac{1 - \frac{5}{16}}{-2 - (-\frac{7}{4})} = \frac{-\frac{11}{16}}{-\frac{1}{4}} = \frac{-11}{4}$$

$$f(-\frac{7}{4}) = (-\frac{7}{4})^2 + (-\frac{7}{4}) - 1 = \frac{5}{16}$$

2) $f(x) = \frac{1}{x-3}$; $[-2, -\frac{3}{2}]$



3) $f(x) = x^2 - x - 1$; $[3, \frac{13}{4}]$

$$f(3) = 3^2 - 3 - 1 = 5$$

$$f(\frac{13}{4}) = (\frac{13}{4})^2 - \frac{13}{4} - 1 = \frac{101}{16}$$

$$m = \frac{5 - \frac{101}{16}}{3 - \frac{13}{4}} = \frac{81}{4}$$

4) $f(x) = -x^2 - x + 1$; $[2, \frac{7}{3}]$

5) $f(x) = 2x^2 - 2x - 1$; $[1, \frac{3}{2}]$

$$f(1) = 2(1)^2 - 2(1) - 1 = -1$$

$$f(\frac{3}{2}) = 2(\frac{3}{2})^2 - 2(\frac{3}{2}) - 1 = \frac{1}{2}$$

$$m = \frac{-1 - \frac{1}{2}}{1 - \frac{3}{2}} = 3$$

6) $f(x) = \frac{1}{x-1}$; $[-4, -\frac{11}{3}]$

7) $f(x) = \frac{1}{x+3}$; $[-1, -\frac{2}{3}]$

$$f(-1) = \frac{1}{-1+3} = \frac{1}{2}$$

$$f(-\frac{2}{3}) = \frac{1}{-\frac{2}{3}+3} = \frac{3}{7}$$

$$m = \frac{\frac{1}{2} - \frac{3}{7}}{-1 - (-\frac{2}{3})} = \frac{-3}{14}$$

8) $f(x) = -\frac{1}{x-1}$; $[-4, -\frac{7}{2}]$

9) The police have accused a driver of breaking the speed limit of 60 miles per hour. As proof, they provide two photographs. One photo shows the driver's car passing a toll booth at exactly 6 PM. The second photo shows the driver's car passing another toll both 31 miles down the highway at exactly 6:30 PM. Does the photo evidence prove that the driver broke the speed limit during this time?

Miles = 31

6pm - 6:30pm = 1/2 hour

$$\text{Speed} = \frac{m}{h} = \frac{31}{\frac{1}{2}} = 62 \text{ mph}$$

Yes, the driver was speeding. He was going 62 mph which is more than 60 mph.

(2)

Name: _____

Date: _____

Linear Functions Practice Problems

1) For $y = \frac{2}{3}x - 6$, which value represents the average rate of change of a line parallel to the equation.

A. $\frac{2}{3}$

B. $-\frac{3}{2}$

C. -6

D. $\frac{1}{6}$

2) For $2y - 13x = 6$, which value represents the average rate of change of a line normal to the equation.

$\frac{2y}{2} = \frac{13x+6}{2}$

$y = \frac{13}{2}x + 3$

$\rightarrow m = -\frac{2}{13}$

A. $-\frac{13}{2}$

B. $\frac{1}{13}$

C. $-\frac{2}{13}$

D. $\frac{13}{6}$

perpendicular

3) Which is an equation of the line normal to $y = 1 - \frac{3}{4}x$ and passes through (3, 4)?

$y - 4 = \frac{4}{3}(x - 3)$

$m = \frac{4}{3}$

A. $y = \frac{4}{3}x - 7$

~~B. $y = -\frac{3}{4}x + \frac{25}{4}$~~

~~C. $y = -1x + 7$~~

D. $y = \frac{4}{3}x$

$y - 4 = \frac{4}{3}x - 4$

$y = \frac{4}{3}x$

4) Which is an equation of the line parallel to $4y - 7x = 8$ and passes through (-4, 0)?

A. $y = \frac{7}{4}x + 7$

$4y = 7x + 8$

$y = \frac{7}{4}x + 2$

~~B. $y = -7x - 28$~~

~~C. $y = -\frac{7}{4}x - 7$~~

~~D. $y = 7x + 28$~~

$m = \frac{7}{4}$

Write the general form of a line for each function.

5) $y = \frac{4}{3}x - 7$
 $\rightarrow = 0$
 $-\frac{4}{3}x + 7$

$y - \frac{4}{3}x + 7 = 0$

6) $y - 1 = 2(x - 2)$

$y - 1 = 2x - 4$

$-2x + 4$

$y - 2x + 3 = 0$

Write the slope-intercept form of a line for each function.

$y = mx + b$

6) $y + 3 = -5(x + 2)$

$y + 3 = -5x - 10$

$-3 \quad -3$

$y = -5x - 13$

7) $4y - 7x = 8$

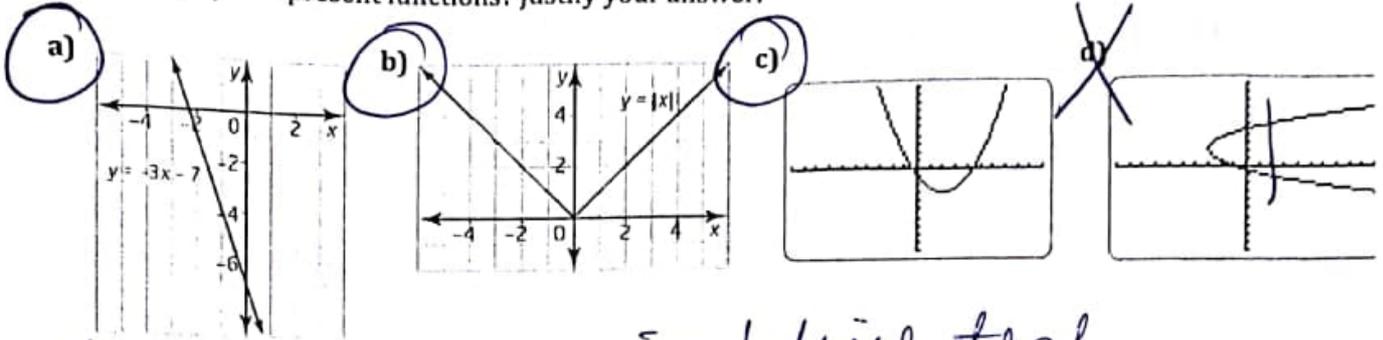
$+7x + 7x$

$\frac{4y = 7x + 8}{4 \quad 4}$

$y = \frac{7}{4}x + 2$

③ Functions, Domain, and Range - Worksheet

1) Which graphs represent functions? Justify your answer.



They pass the vertical line test

2) Is each relation a function? Explain and make a rough sketch of the graph of each.

a) $y = x - 5$ Yes
Linear function



b) $y = 2(x - 1)^2 - 2$ Yes
Quadratic function



c) $x^2 + y^2 = 4$ NO
Circle
 $y = \pm \sqrt{-x^2 + 4}$



3) State the domain and range. Represent as a table and graph. Then state if it is a function.

a) $\{(-5, 4), (-4, -1), (-2, 1), (0, 4), (1, 3)\}$

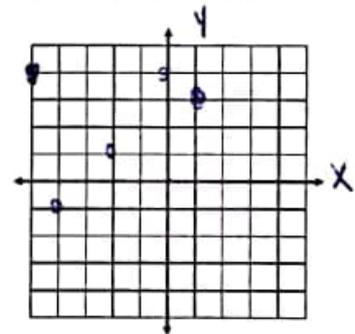
Domain:

$\{-5, -4, -2, 0, 1\}$

Range:

$\{-1, 1, 3, 4\}$

x	y
-5	4
-4	-1
-2	1
0	4
1	3



Is this relation a function?

yes!

4

b) $\{(-3, -4), (-1, 2), (0, 0), (-3, 5), (2, 4)\}$

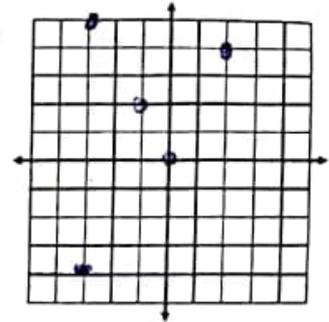
Domain:

$\{-3, -1, 0, 2\}$

Range:

$\{-4, 2, 0, 5, 4\}$

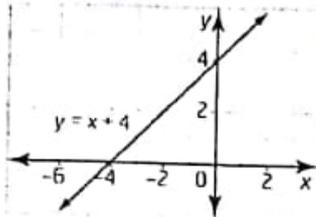
x	y
-3	-4
-1	2
0	0
-3	5
2	4



Is this relation a function? **NO!**

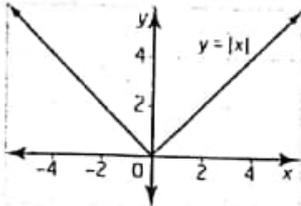
4) State the domain and range of each relation. Then state if the relation is a function.

a)



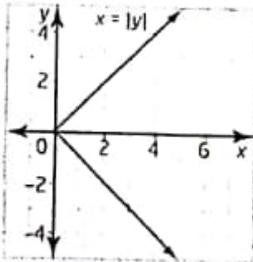
Function
 $D: \mathbb{R}$

b)



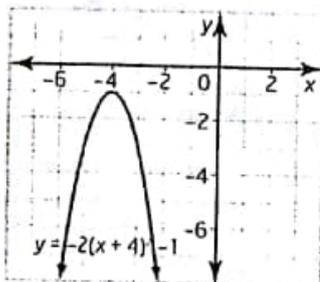
Function
 $D: \mathbb{R}$

c)



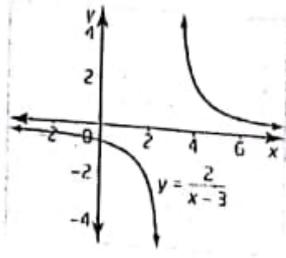
Not a function
 $D: x \geq 0$

d)



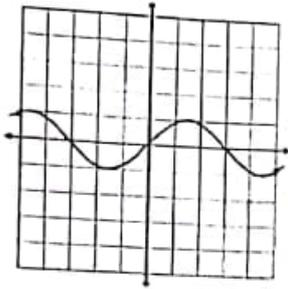
Function
 $D: \mathbb{R}$

e)



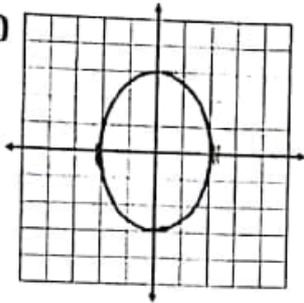
Function
 $D: \mathbb{R}$ except $x=3$

f)



Function
 $D = \mathbb{R}$

g)



Not a function
 $D: -2 \leq x \leq 2$

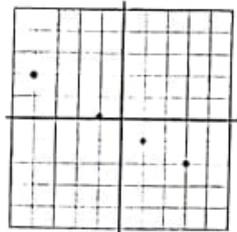
5) Which of the following relations are functions?

a)

x	y
2	-3
-1	0
5	5
3	2
2	1

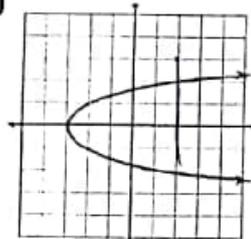
NO

b)



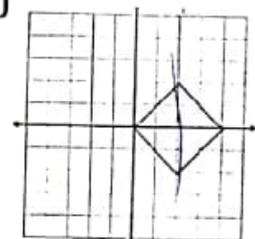
Yes

c)



NO

d)



NO

6

odds only!

Evaluating Functions

Evaluate each function.

Name _____

Date _____ Period _____

1) $h(t) = |t+2| + 3$; Find $h(6)$

$$h(6) = |6+2| + 3 = 11$$

2) $g(a) = 3^{3a-2}$; Find $g(1)$

3) $w(t) = -2t + 1$; Find $w(-7)$

$$w(-7) = -2(-7) + 1 = 15$$

4) $g(x) = 3x - 3$; Find $g(-6)$

5) $h(n) = -2n^2 + 4$; Find $h(4)$

$$h(4) = -2(4)^2 + 4 = -28$$

6) $h(t) = -2 \cdot 5^{-t-1}$; Find $h(-2)$

7) $f(x) = x^2 - 3x$; Find $f(-8)$

$$f(-8) = (-8)^2 - 3(-8) = 88$$

8) $p(a) = -4^{3a}$; Find $p(-1)$

9) $p(t) = 4t - 5$; Find $p(t-2)$

$$\begin{aligned} p(t-2) &= 4(t-2) - 5 \\ &= 4t - 8 - 5 \\ &= 4t - 13 \end{aligned}$$

10) $g(a) = 4a$; Find $g(2a)$

11) $w(n) = 4n + 2$; Find $w(3n)$

$$\begin{aligned} w(3n) &= 4(3n) + 2 \\ &= 12n + 2 \end{aligned}$$

12) $w(a) = a + 3$; Find $w(a+4)$

13) $h(x) = 4x - 2$; Find $h(x+2)$

$$\begin{aligned} h(x+2) &= 4(x+2) - 2 \\ &= 4x + 8 - 2 \\ &= 4x + 6 \end{aligned}$$

14) $k(a) = -4^{3a+2}$; Find $k(a-2)$

15) $g(n) = n^3 - 5n^2$; Find $g(-4n)$

$$\begin{aligned} g(-4n) &= (-4n)^3 - 5(-4n)^2 \\ &= -64n^3 - 5(16n^2) \\ &= -64n^3 - 80n^2 \end{aligned}$$

16) $f(n) = n^2 - 2n$; Find $f(n^2)$

17) $p(a) = a^3 - 5$; Find $p(x-4)$

$$\begin{aligned} p(x-4) &= (x-4)^3 - 5 \\ &= x^3 - 8x^2 + 16x - 4x^2 + 32x - 64 - 5 \\ &= x^3 - 12x^2 + 48x - 69 \end{aligned}$$

18) $h(t) = 2 \cdot 3^{t+3}$; Find $h(4+t)$

7

Difference quotient review

$$\frac{f(x+h) - f(x)}{h}$$

1) Given $f(x) = 4x^2$, find the difference quotient.

$$\frac{4(x+h)^2 - 4x^2}{h} = \frac{4(x^2 + 2xh + h^2) - 4x^2}{h} = \frac{4x^2 + 8xh + 4h^2 - 4x^2}{h}$$

$$\frac{8xh + 4h^2}{h} = \frac{h(8x + 4h)}{h} = 8x + 4h$$

2) Given $f(x) = 2x^2 - x$, find the difference quotient.

$$\frac{[2(x+h)^2 - (x+h)] - [2x^2 - x]}{h} = \frac{2(x^2 + 2xh + h^2) - x - h - 2x^2 + x}{h}$$

$$\frac{2x^2 + 4xh + 2h^2 - x - h - 2x^2 + x}{h} = \frac{4xh + 2h^2 - h}{h} = \frac{h(4x + 2h - 1)}{h}$$

$$= 4x^2 + 2h - 1$$

3) Given $f(x) = 9 - 2x^3$, find the difference quotient.

$$\frac{[9 - 2(x+h)^3] - [9 - 2x^3]}{h} = \frac{9 - 2(x^3 + 3x^2h + 3xh^2 + h^3) - 9 + 2x^3}{h}$$

$$= \frac{9 - 2x^3 - 6x^2h - 6xh^2 - 2h^3 - 9 + 2x^3}{h} = \frac{-6x^2h - 6xh^2 - 2h^3}{h}$$

$$= \frac{h(-6x^2 - 6xh - 2h^2)}{h} = -6x^2 - 6xh - 2h^2$$

$(x+h)^3 = (x+h)(x+h)(x+h)$
 $= (x+h)(x^2 + 2xh + h^2)$
 $= x^3 + 3x^2h + 3xh^2 + h^3$

(8)

Name: _____
Unit: Functions

Date: _____
CW: Finding the Domain Algebraically

Directions: Find, algebraically the domain of each function. Restrict the domain wherever possible. Odds only.

1) $d(y) = y + 3$

\mathbb{R}
(linear)

2) $g(k) = 2k^2 + 4k - 6$

3) $b(n) = \sqrt{2n - 8}$

$$\begin{aligned} 2n - 8 &\geq 0 \\ +8 &\quad +8 \\ \hline 2n &\geq 8 \\ \frac{2n}{2} &\geq \frac{8}{2} \\ n &\geq 4 \end{aligned}$$

4) $m(t) = \sqrt{9 - 3t}$

5) $u(x) = \frac{x - 5}{2x + 4}$

$$\begin{aligned} 2x + 4 &= 0 \\ 2x &= -4 \\ x &= -2 \end{aligned}$$

6) $a(r) = r + \frac{1}{r - 1}$

\mathbb{R} except $x = -2$

7) $y(c) = \frac{2}{c^2 + 3c}$

8) $q(w) = \frac{w + 4}{w^2 - 25}$

$$c^2 + 3c = 0$$

$$c(c + 3) = 0$$

$$\begin{aligned} c = 0 \quad c + 3 = 0 \\ c = -3 \end{aligned}$$

\mathbb{R} except $x = 0$ and $x = -3$

9) * odds only!

$$9) g(x) = x^2 - 2x - 10$$

quadratic
 \mathbb{R}

$$10) h(x) = \frac{1}{x^2 - 12x + 35}$$

$$* 11) f(x) = \frac{x}{\sqrt{x+3}}$$

$$x+3 > 0$$

$$x > -3$$

$$12) t(v) = \sqrt{v^2 + 2v - 8}$$

$$13) h(x) = \sqrt{x^2 - 4x - 5}$$

$$x^2 - 4x - 5 \geq 0$$

$$(x-5)(x+1) \geq 0$$

$$x-5 \geq 0$$

$$x \geq 5$$

$$x+1 \leq 0$$

$$x \leq -1$$

* Switch

$$14) f(x) = \frac{1}{\sqrt{4-x^2}}$$