

Name Answer Key
Ms. Schmidt

Date _____
Intermediate Algebra

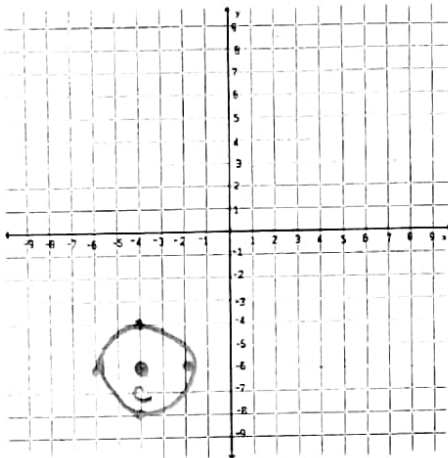
Review for Past Units

Kick off-

- 1) Write the equation of the circle whose center is $(-4, -6)$ and has a point $(-2, -6)$ on the circle.

$$(x + 4)^2 + (y + 6)^2 = 4$$
$$(-2 + 4)^2 + (-6 + 6)^2 = 4$$

- 2) Graph the equations to number 1!

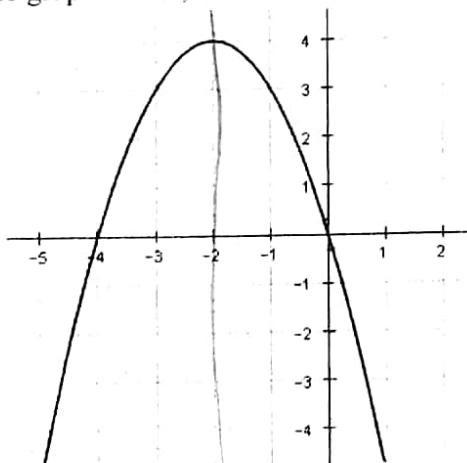


$$C \rightarrow (-4, -6)$$
$$r = \sqrt{4} = 2$$

- 3) Write the equation of the circle in standard form: $x^2 + y^2 - 2x + 24y + 120 = 0$

$$x^2 - 2x + y^2 + 24y + 120 = 0$$
$$x^2 - 2x + y^2 + 24y = -120$$
$$ + 1$$
$$ + 144$$
$$(x - 1)^2 + (y + 12)^2 = 25$$

- 4) Using the graph below, determine the following:



- A) The axis of symmetry

$$x = -2$$

- B) State the maximum point

$$(-2, 4)$$

- C) The roots of the equation.

$$(-4, 0) + (0, 0)$$

Operations with Polynomials

Given: $f(x) = 3x - 1$, $g(x) = x - 9$, $k(x) = x^2 - 4x + 4$, $m(x) = 3x^2 + 8x + 5$ find each of the following.

1) $f(x) + k(x)$

$$\begin{aligned} 3x - 1 + x^2 - 4x + 4 \\ x^2 - x + 3 \end{aligned}$$

2) Subtract $f(x)$ from $m(x)$ \swarrow 1st

$$\begin{aligned} (3x^2 + 8x + 5) - (3x - 1) \\ 3x^2 + 8x + 5 - 3x + 1 \\ 3x^2 + 5x + 6 \end{aligned}$$

3) $f(x) \cdot g(x)$

$$\begin{aligned} (3x - 1)(x - 9) \\ 3x^2 - 27x - x + 9 \\ 3x^2 - 28x + 9 \end{aligned}$$

4) $m(x) - k(x)$

$$\begin{aligned} (3x^2 + 8x + 5) - (x^2 - 4x + 4) \\ 3x^2 + 8x + 5 - x^2 + 4x - 4 \\ 2x^2 + 12x + 1 \end{aligned}$$

5) Subtract $g(x)$ from $k(x)$ \swarrow 1st

$$\begin{aligned} (x^2 - 4x + 4) - (x - 9) \\ x^2 - 4x + 4 - x + 9 \\ x^2 - 5x + 13 \end{aligned}$$

6) $m(x) + g(x)$

$$\begin{aligned} (3x^2 + 8x + 5) + (x - 9) \\ 3x^2 + 9x - 4 \end{aligned}$$

7) $g(x) \cdot f(x)$

$$\begin{aligned} (x - 9)(3x - 1) \\ 3x^2 - x - 27x + 9 \\ 3x^2 - 28x + 9 \end{aligned}$$

8) Subtract $k(x)$ from $m(x)$ \swarrow 1st

$$\begin{aligned} (3x^2 + 8x + 5) - (x^2 - 4x + 4) \\ 3x^2 + 8x + 5 - x^2 + 4x - 4 \\ 2x^2 + 12x + 1 \end{aligned}$$

Given If $f(x) = x - 4$, $g(x) = 4x + 8$, $k(x) = 2x - 1$, $m(x) = 3x + 6$ find each of the following:

9) $g(f(2))$

$$f(2) = 2 - 4 = -2$$

$$g(-2) = 4(-2) + 8 = \boxed{0}$$

10) $g(f(x))$

$$4(x - 4) + 8$$

$$4x - 16 + 8$$

$$4x - 8$$

11) $k(m(-4))$

$$m(-4) = 3(-4) + 6 = -6$$

$$k(-6) = 2(-6) - 1 = \boxed{-13}$$

12) $k(m(x))$

$$2(3x + 6) - 1$$

$$6x + 12 - 1$$

$$6x + 11$$

13) $k(f(3))$

$$f(3) = 3 - 4 = -1$$

$$k(-1) = 2(-1) - 1 = \boxed{-3}$$

14) $k(f(x))$

$$2(x - 4) - 1$$

$$2x - 8 - 1$$

$$2x - 9$$

15) $m(g(0))$

$$g(0) = 4(0) + 8 = 8$$

$$m(8) = 3(8) + 6 = \boxed{30}$$

16) $m(g(x))$

$$3(4x + 8) + 6$$

$$12x + 24 + 6$$

$$12x + 30$$

Systems of Equations

17) Is $(-3, -6)$ a solution of the system of equations: $-4x + y = 6$

$$-5x - y = 21$$

$$\begin{aligned} -4(-3) + (-6) &= 6 \\ 6 &= 6 \checkmark \end{aligned}$$

$$\begin{aligned} -5(-3) - (-6) &= 21 \\ 21 &= 21 \checkmark \end{aligned}$$

yes!

18) Is $(1, -2)$ a solutions of the system of equations: $-5x + y = -2$

$$-3x + 6y = -12$$

$$\begin{aligned} -5(1) + (-2) &= -2 \\ -7 &\neq -2 \\ \text{NO!} \end{aligned}$$

19) Is $(3, -4)$ a solution of the system of equations: $-7x - 2y = -13$

$$x - 2y = 11$$

$$\begin{aligned} -7(3) - 2(-4) &= -13 \\ -13 &= -13 \\ \checkmark \end{aligned}$$

$$\begin{aligned} (3) - 2(-4) &= 11 \\ 11 &= 11 \\ \checkmark \end{aligned}$$

yes!

20) Is $(-5, 4)$ a solution of the system of equations: $2x - 3y = -1$

$$y = x - 1$$

$$\begin{aligned} 2(-5) - 3(4) &= -1 \\ -22 &\neq -1 \\ \text{NO!} \end{aligned}$$

Solving Equations

21) Solve and check: $2x - 5 + 7x = 11 - 3x + 4x$

$$\begin{array}{r} 9x - 5 = 11 + x \\ -x \quad -x \\ \hline 8x - 5 = 11 \\ +5 \quad +5 \\ \hline 8x = 16 \\ \frac{8x}{8} = \frac{16}{8} \\ x = 2 \end{array}$$

Check

$$\begin{aligned} 2(2) - 5 + 7(2) &= 11 - 3(2) + 4(2) \\ 13 &= 13 \\ &\checkmark \end{aligned}$$

22) Solve and Check: $-2(1 - 7y) = 8(y - 7)$

$$\begin{array}{r} -2 + 14y = 8y - 56 \\ -8y \quad -8y \\ \hline -2 + 6y = -56 \\ +2 \quad +2 \\ \hline 6y = -54 \\ \frac{6y}{6} = \frac{-54}{6} \\ y = -9 \end{array}$$

Check

$$\begin{aligned} -2(1 - 7(-9)) &= 8(-9 - 7) \\ -128 &= -128 \\ &\checkmark \end{aligned}$$

23) Solve and check: $8x + 16x - 12 = 24x - 16 + 4$

$$\begin{array}{r} 24x - 12 = 24x - 12 \\ -24x \quad -24x \\ \hline -12 = -12 \end{array}$$

Many solutions!

24) Solve and check: $5(2x + 6) = -4(-5 - 2x) + 3x$

$$\begin{array}{r} 10x + 30 = 20 + 8x + 3x \\ -10x \quad -10x \\ \hline 30 = 20 + x \\ -20 \quad -20 \\ \hline 10 = x \end{array}$$

Check

$$\begin{aligned} 5(2(10) + 6) &= -4(-5 - 2(10)) + 3(10) \\ 130 &= 130 \\ &\checkmark \end{aligned}$$